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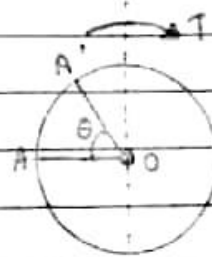
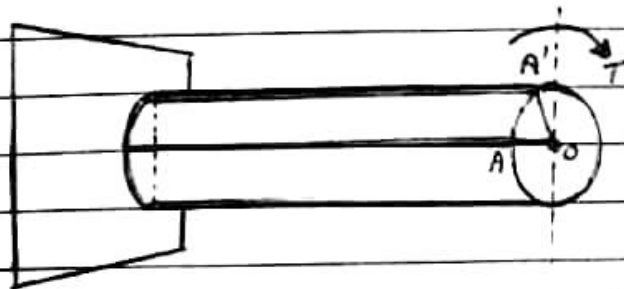
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D.K. College, Dumkoon (Buxar), Notes for
B.Sc part 1, paper 1 (A)

Question:- Q1: Write notes on Torsion of
Shafts with diagrams and classification

Answer:- Torsion means twisting a structural member when it is loaded by couple that produces rotation about longitudinal axis.

• If τ be intensity of shear stress, on any layer at a distance r from the centre of shaft, then

$$\frac{T}{J} = \frac{\tau}{r} = \frac{G\theta}{L}$$



Torsion in shaft and combined stresses

Sign Convention:-

• Sign convention of torque can be explained by right hand thumb rule.

- A positive torque is that in which there is tightening effect of nut on the bolt. from either side of the cross-section. If torque is applied in the direction of right hand fingers then right hand thumb's direction represents movement of the nut.

$T = \text{Torque}$

- Rate of twist:

$$\frac{(\theta)}{L} \frac{\theta}{1} = \frac{T}{GJ}$$

- Total angle of twist:

$$\theta = \frac{TL}{GJ}$$

Where, $T = \text{Torque,}$

- $J = \text{Polar moment of Inertia}$
- $G = \text{Modulus of rigidity,}$
- $\theta = \text{Angle of twist}$
- $L = \text{Length of shaft,}$
- $GJ = \text{Torsional rigidity}$

$$\frac{GJ}{L} \rightarrow$$

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- Torsional stiffness:

$$\frac{T}{\theta} \rightarrow$$

- Torsional Flexibility

$$\frac{ER}{L} \rightarrow$$

- Axial stiffness;

$$\frac{L}{EA} \rightarrow$$

Moment of Inertia about polar Axis:

- For solid circular shaft;

$$J = \frac{\pi d^4}{32}, T_{max} = \frac{16T}{\pi d^3}$$

- For hollow circular shaft:

$$J = \frac{\pi}{32} (d_o^4 - d_i^4)$$

Power Transmitted in the shaft:

- Power transmitted by shaft:

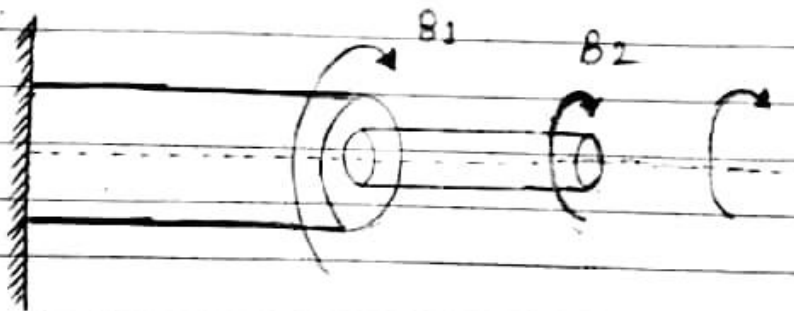
$$P = \frac{2\pi NT}{60000} \text{ kW}$$

Where, N = Rotation per minute.

Compound shaft

An improved type of compound coupling for connecting in series and parallel are given below.

1. Series connection: Series connection of compound shaft as shown in figure. Due to series connection the torque on shaft 1 will be equal to shaft 2 and the total angular deformation will be equal to the sum of deformation of 1st shaft and 2nd shaft.



Series connection

$$\theta = \theta_1 + \theta_2$$

$$T = T_1 = T_2$$

Therefore,

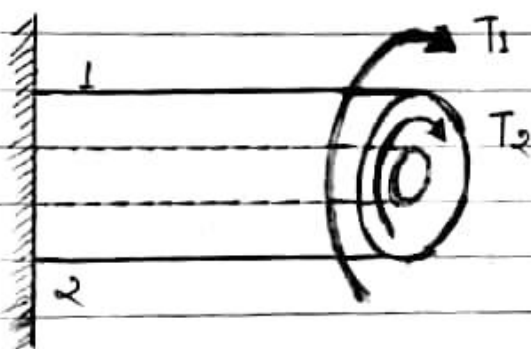
$$\theta = \frac{TL_1}{GJ_1} + \frac{TL_2}{GJ_2}$$

Where,

θ_1 = Angular deformation of 1st shaft

θ_2 = Angular deformation of 2nd shaft

1. Parallel Connection :- Parallel connection of compound shaft as shown in figure. Due to parallel connection of compound shaft the total torque will be equal to the sum of torque of shaft 1 and torque of shaft 2 and the deflection will be same in both the shafts.



Parallel Connection

$$\theta_1 = \theta_2$$

$$T = T_1 + T_2$$

Therefore,

$$\frac{T_1 L}{G J_1} = \frac{T_2 L}{G J_2}$$

Strain energy (U) stored in shaft due to torsion:

$$U = \frac{1}{2} T \cdot \theta = \frac{1}{2} \frac{T^2}{G J} = \frac{\tau^2 \max}{4G} \cdot \text{Volume of shaft}$$

• G = Shear Modulus

• T = Torque

• J = Moment of inertia about polar axis.